



# Introduction to Radar Systems

## Radar Antennas

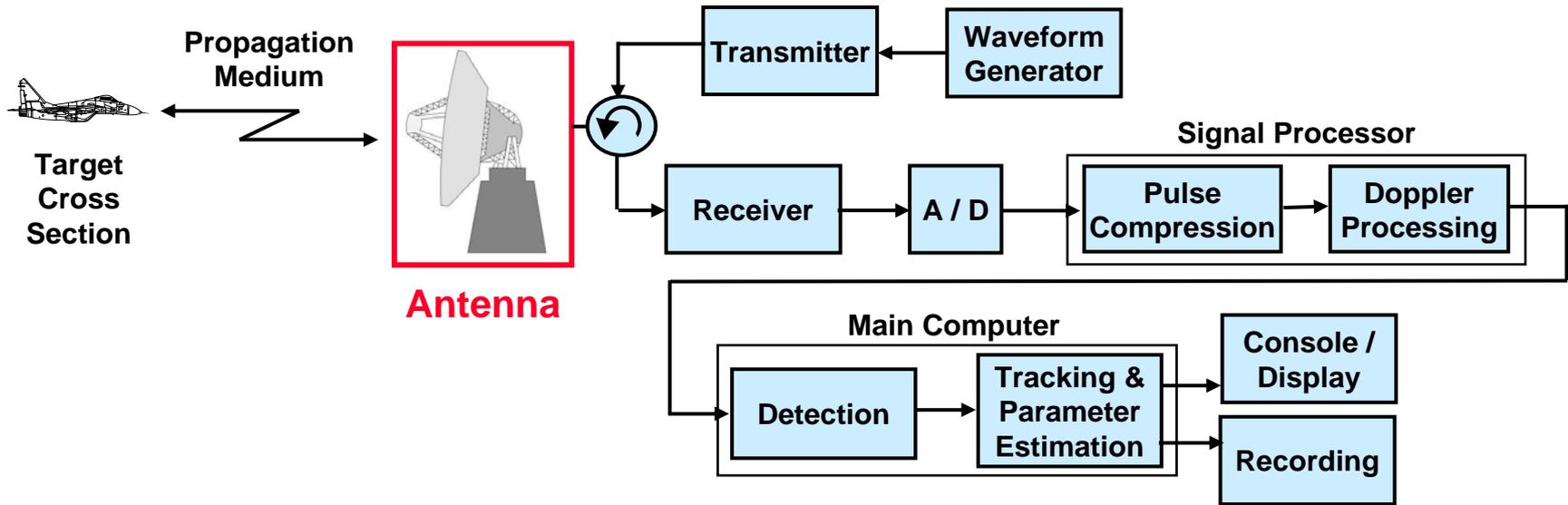


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# Focus



Track  
Radar  
Equation

$$S / N = \frac{P_t G^2 \lambda^2 \sigma}{(4 \pi)^3 R^4 k T_s B_n L}$$

**G = Gain**

**A<sub>e</sub> = Effective Area**

*This  
Lecture*

Search  
Radar  
Equation

$$S / N = \frac{P_{av} A_e t_s \sigma}{4 \pi \Omega R^4 k T_s L}$$

**T<sub>s</sub> = System Noise  
Temperature**

**L = Losses**

*Radar  
Equation  
Lecture*



# Antenna Definition

- “Means for radiating or receiving radio waves”
  - A radiated electromagnetic wave consists of electric and magnetic fields which jointly satisfy Maxwell’s Equations
- Transitional structure between guiding device and free space

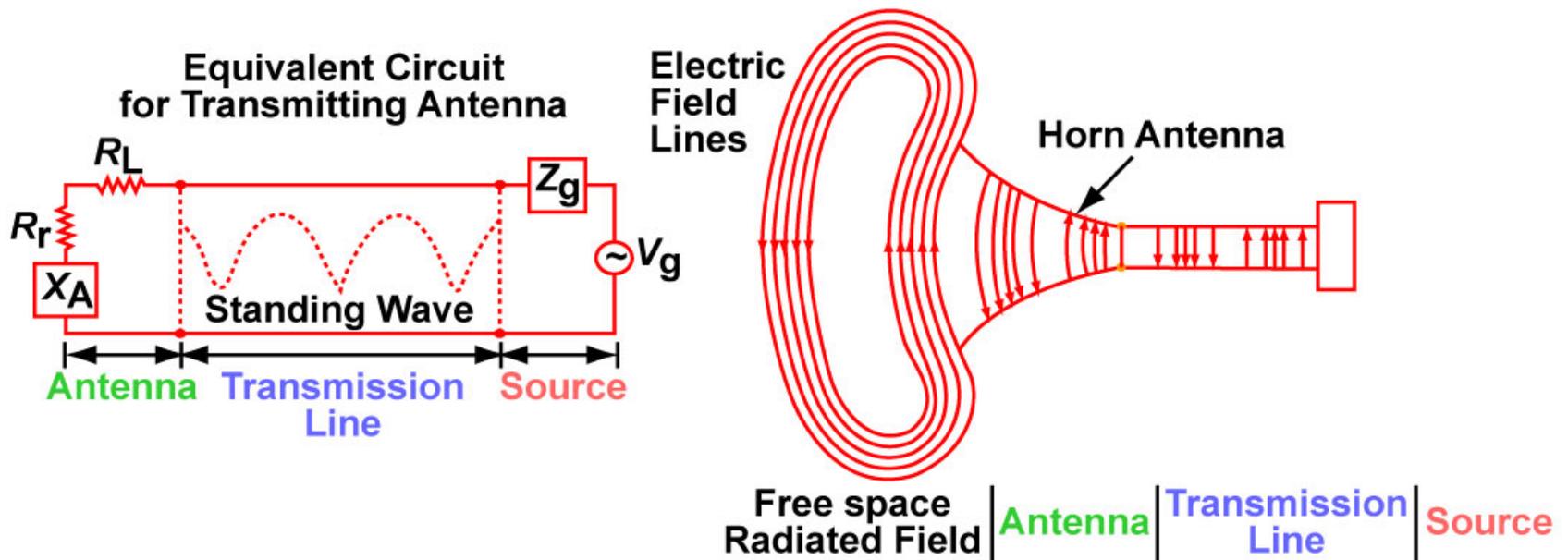
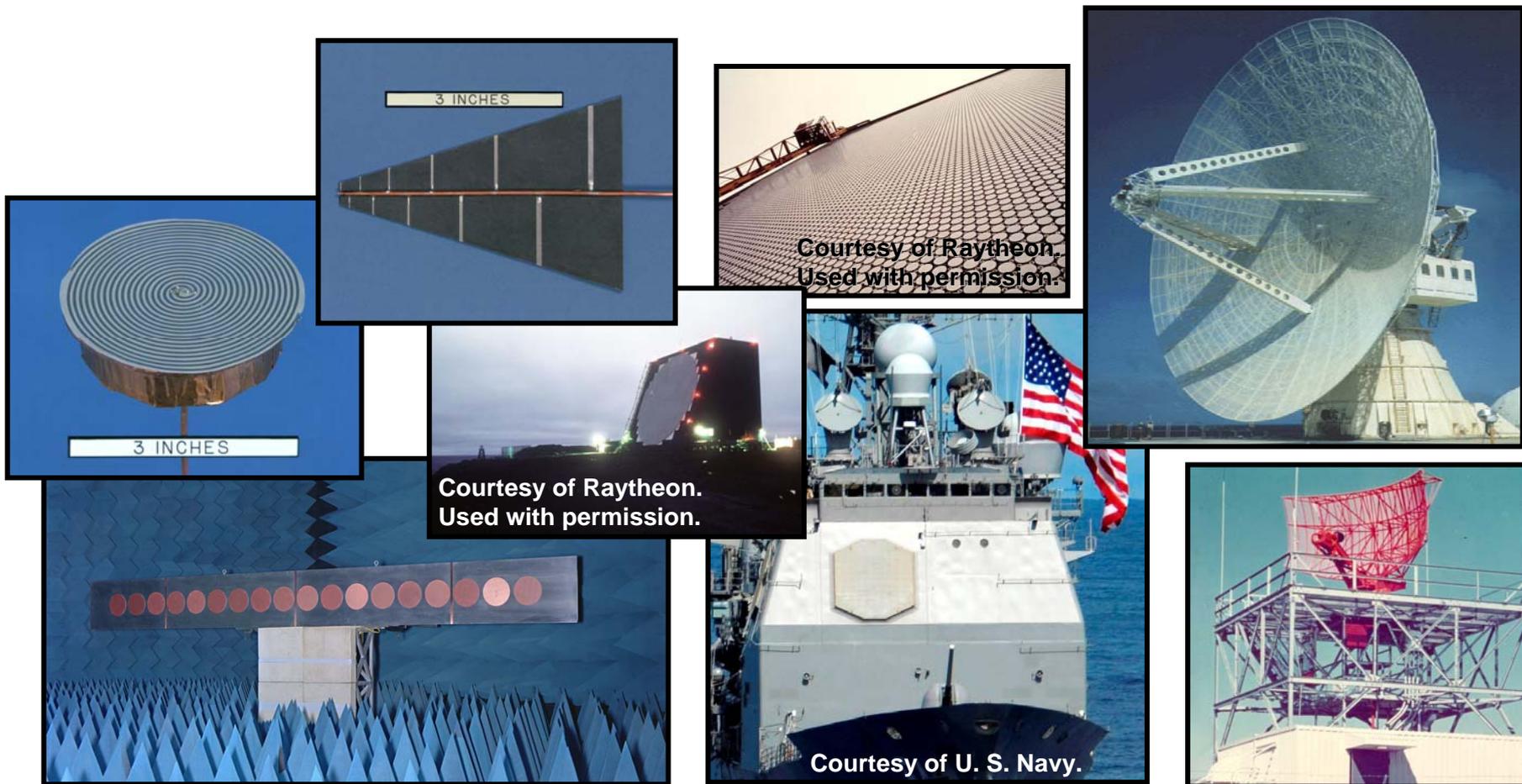


Figure by MIT OCW.



# Antenna Characteristics

- Accentuates radiation in some directions, suppresses in others
- Designed for both directionality and maximum energy transfer





# Outline

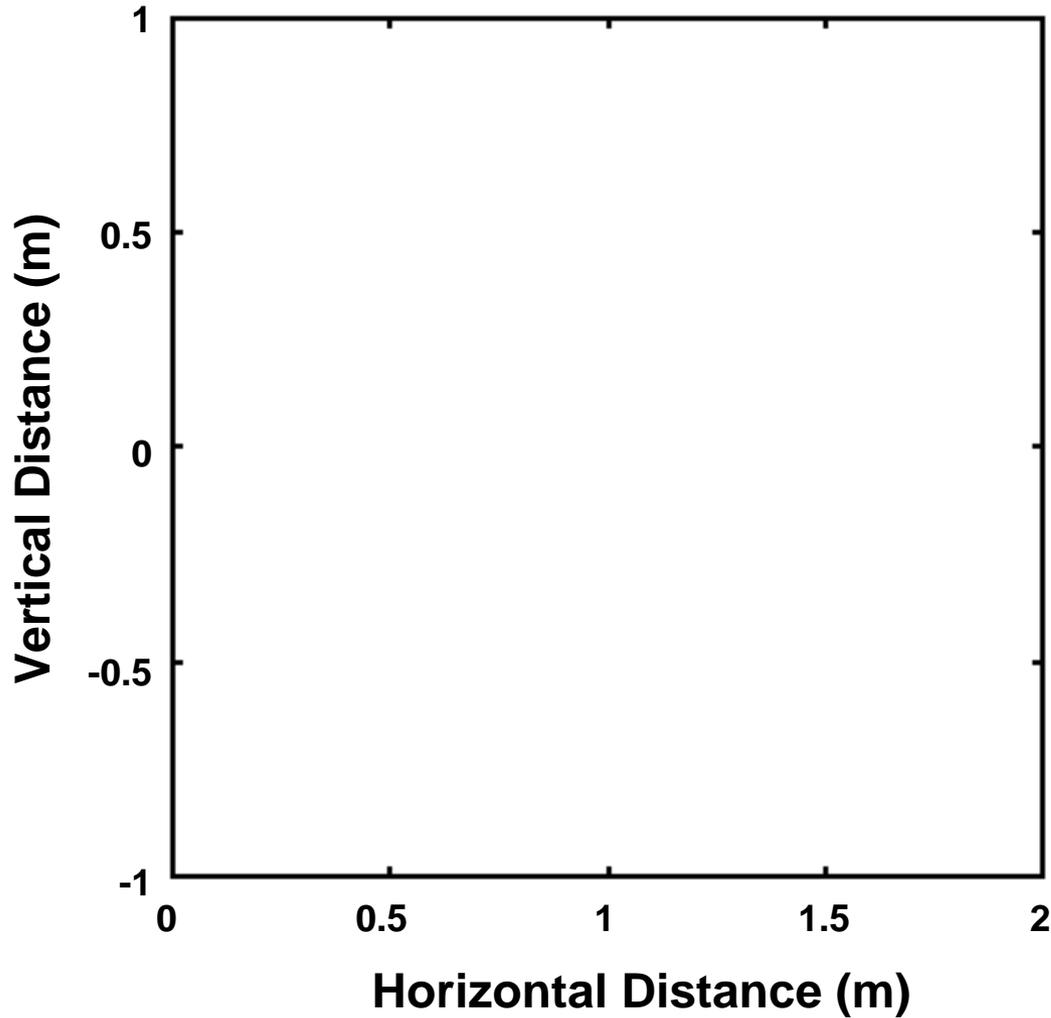
- Introduction
- ➔ • **Fundamental antenna concepts**
- Reflector antennas
- Phased array antennas
- Summary



# Radiation

Dipole\* →

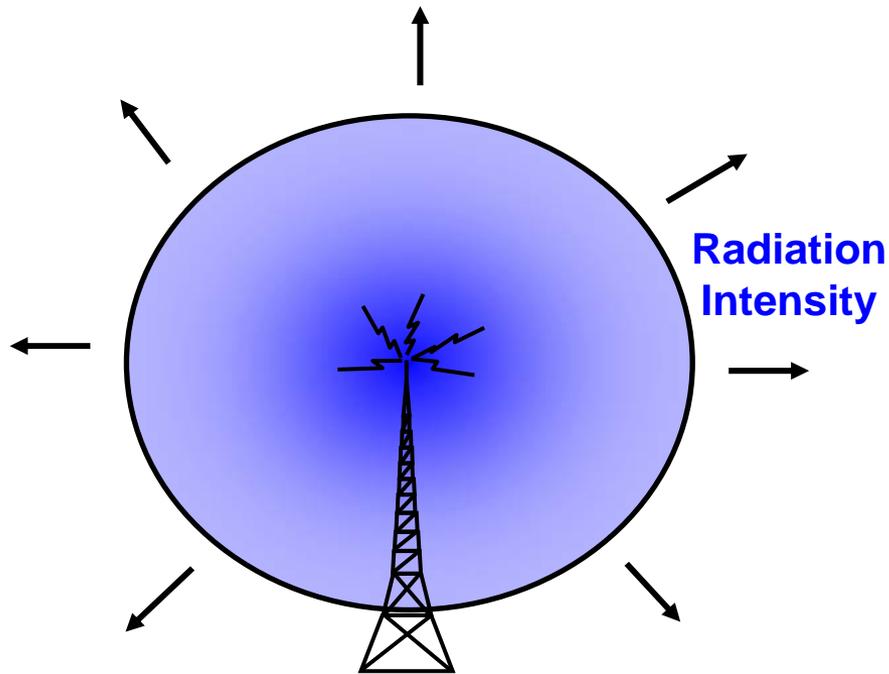
\*driven by  
oscillating  
source



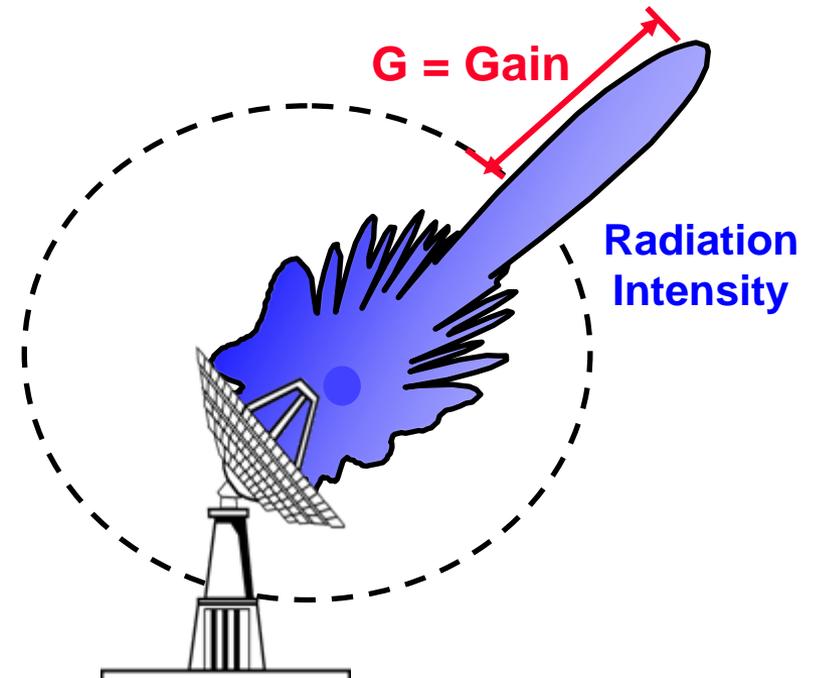


# Antenna Gain

## Isotropic Antenna



## Directional Antenna



- Same power is radiated
- **Radiation intensity** is power density over sphere (watt/steradian)
- **Gain** is radiation intensity over that of an isotropic source



# Antenna Pattern

- Pattern is a plot of gain versus angle
- Dipole example

$$G(\theta) = 1.643 \left[ \frac{\cos^2\left(\frac{\pi}{2} \cos\theta\right)}{\sin^2\theta} \right]$$

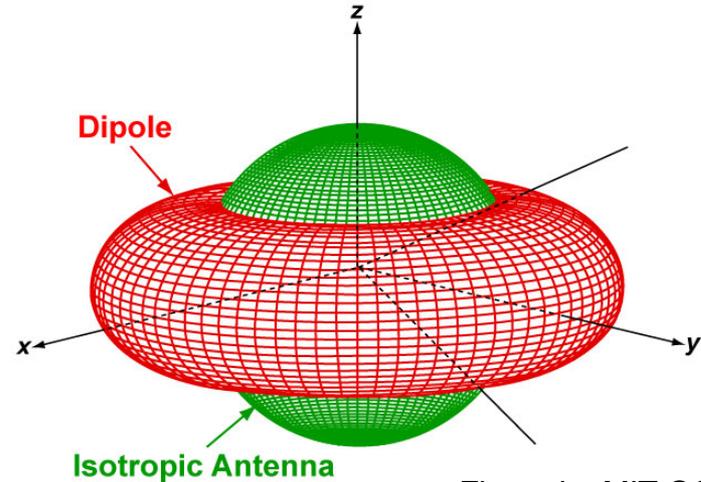
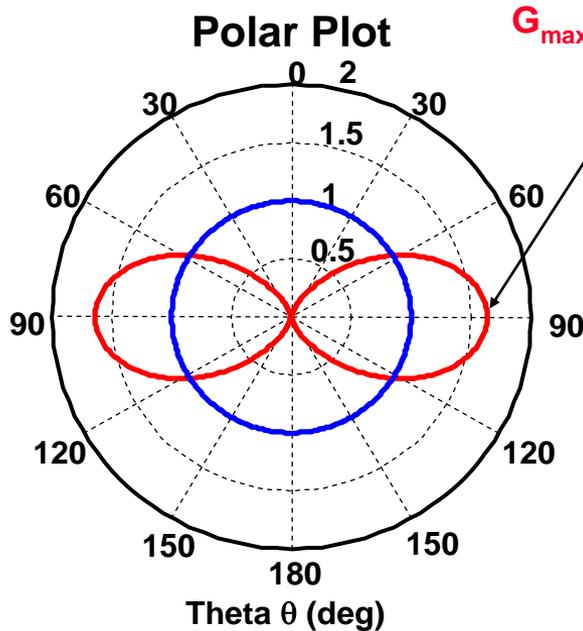
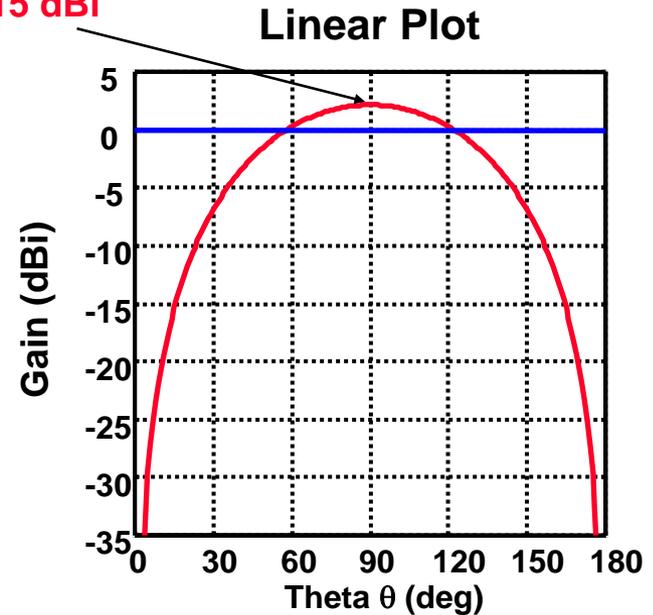


Figure by MIT OCW.



$$G_{\max} = 1.64 = 2.15 \text{ dBi}$$





# Antenna Pattern Characteristics

## Parabolic Reflector Antenna

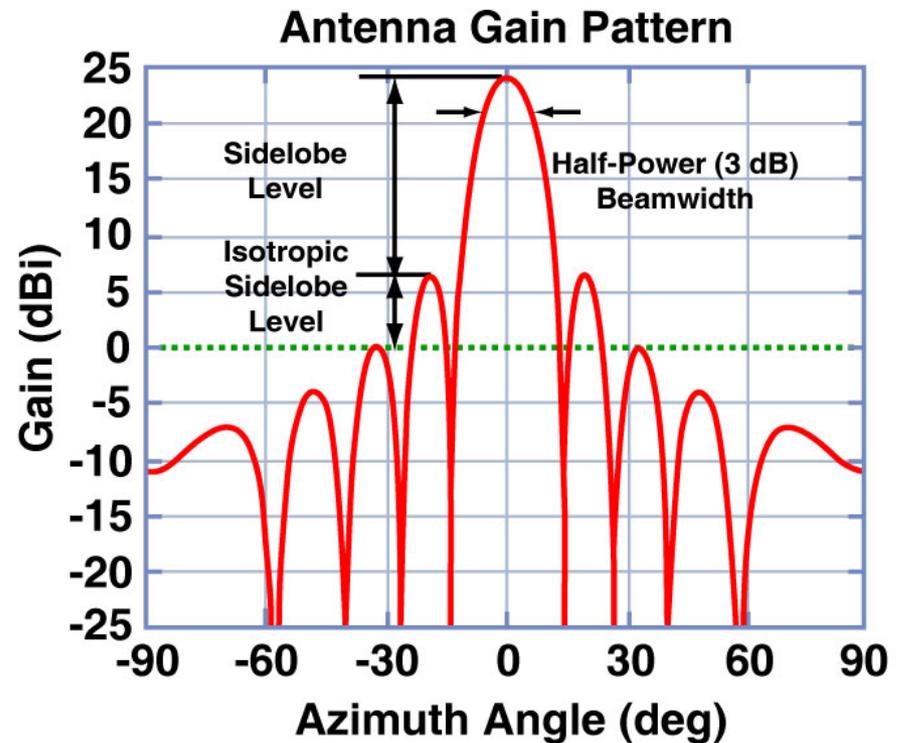
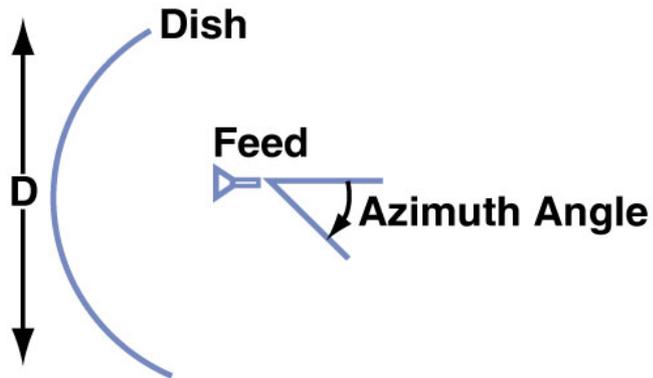


Figure by MIT OCW.

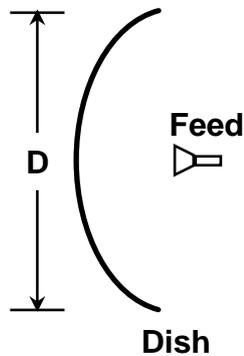
Aperture diameter  $D$ : 5 m  
Frequency: 300 MHz  
Wavelength: 1 m

Gain: 24 dBi  
Isotropic Sidelobe Level: 6 dBi  
Sidelobe Level: 18 dB  
Half-Power Beamwidth: 12 deg



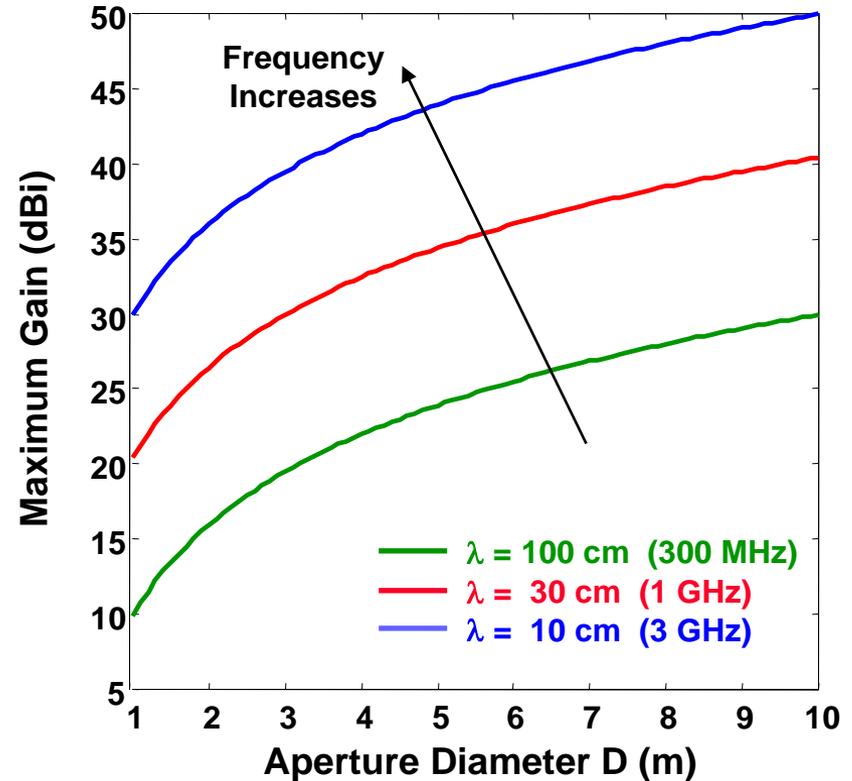
# Effect of Aperture Size on Gain

## Parabolic Reflector Antenna



$$\text{Gain} = \frac{4\pi A_e}{\lambda^2} \leftarrow \text{Effective Area}$$
$$\approx \frac{4\pi A}{\lambda^2} \leftarrow \text{Rule of Thumb (Best Case)}$$
$$= \left( \frac{\pi D}{\lambda} \right)^2$$

## Gain vs Diameter



**Gain increases as aperture becomes electrically larger (diameter is a larger number of wavelengths)**



# Reflector Comparison

## Kwajalein Missile Range Example

**ALTAIR**  
45.7 m diameter



Operating frequency: 162 MHz (VHF)  
Wavelength  $\lambda$ : 1.85 m

**Diameter electrical size:  $25 \lambda$**

Gain: 34 dB

Beamwidth: 2.8 deg

scale by  
 $1/3$



**MMW**  
13.7 m diameter



Operating frequency: 35 GHz (Ka)  
Wavelength  $\lambda$ : 0.0086 m

**Diameter electrical size:  $1598 \lambda$**

Gain: 70 dB

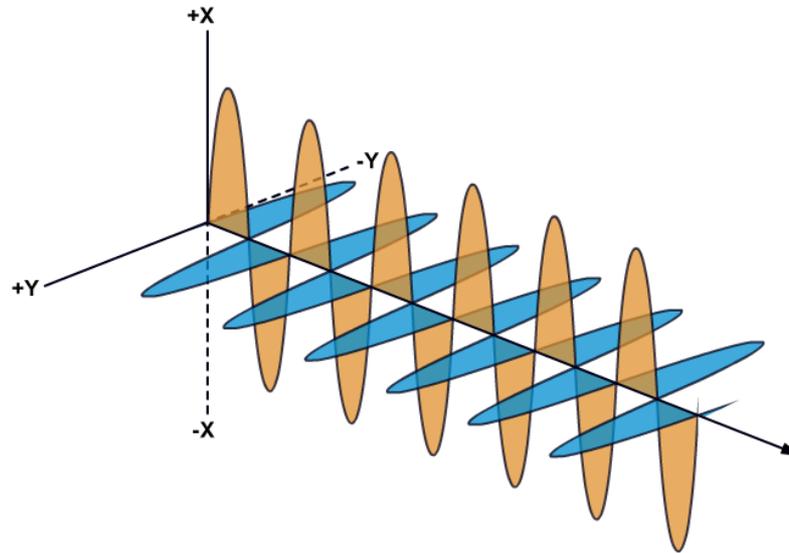
Beamwidth: 0.00076 deg



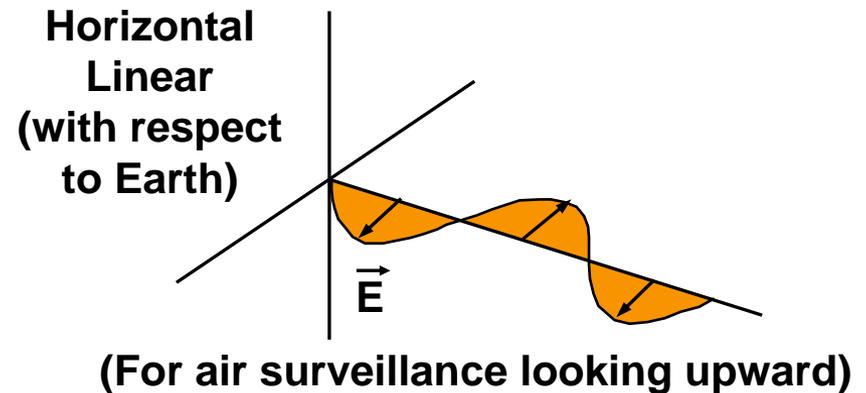
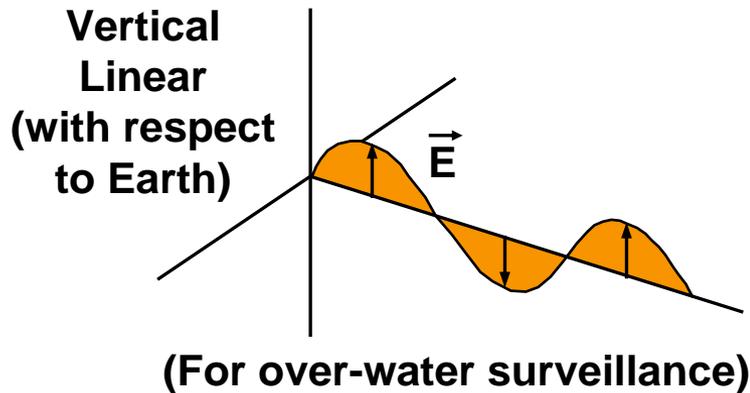
# Polarization

- Defined by behavior of the electric field vector as it propagates in time

Electromagnetic Wave



 Electric Field  
 Magnetic Field





# Circular Polarization (CP)

- “Handed-ness” is defined by observation of electric field along propagation direction
- Used for discrimination, polarization diversity, rain mitigation

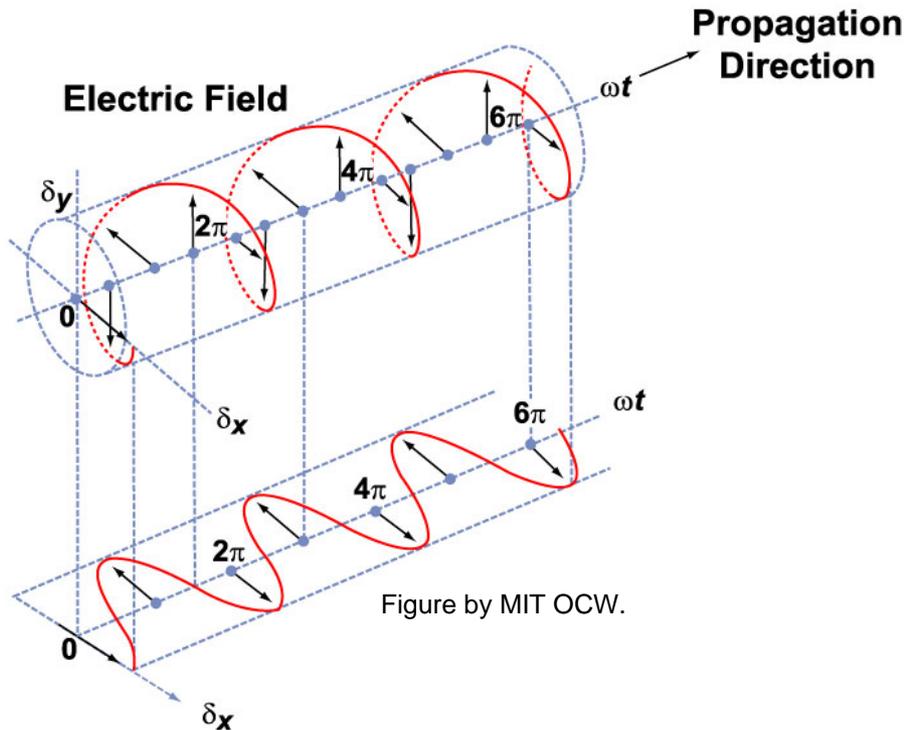
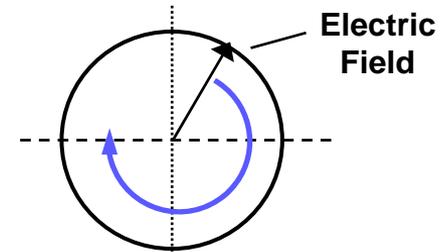


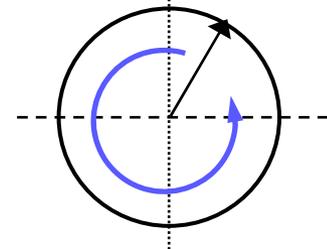
Figure by MIT OCW.

Propagation Direction  
Into Paper

Right-Hand  
(RHCP)



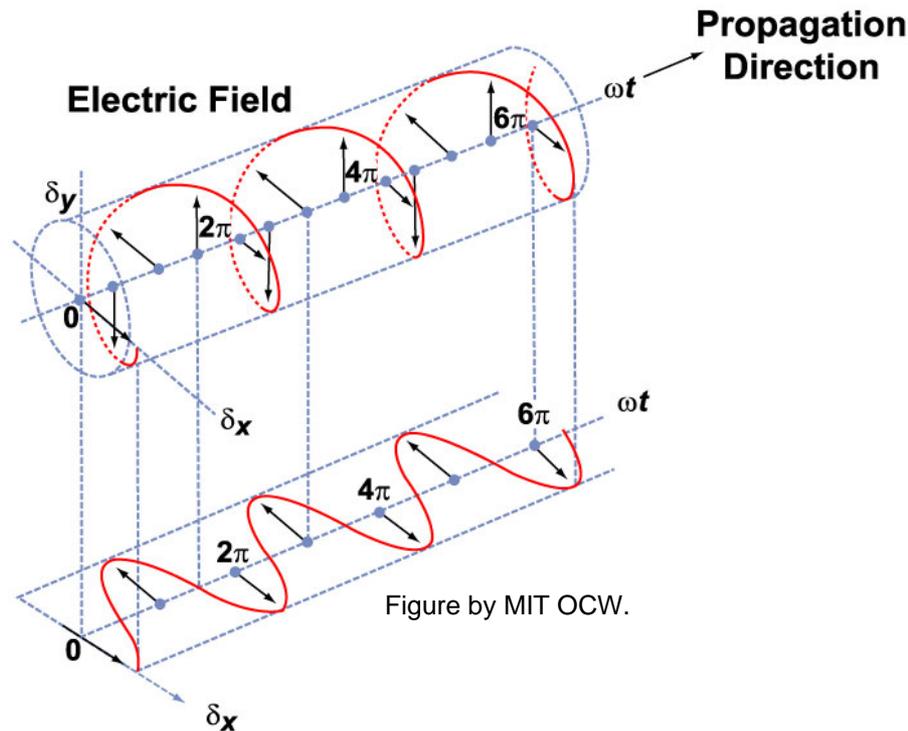
Left-Hand  
(LHCP)





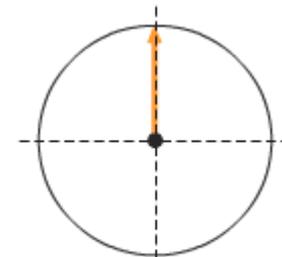
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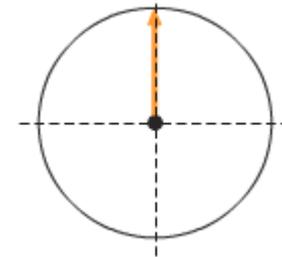


Propagation Direction  
Into Paper

Right-Hand  
(RHCP)



Left-Hand  
(LHCP)



Electric Field

MIT Lincoln Laboratory



# Field Regions

## Reactive Near-Field Region

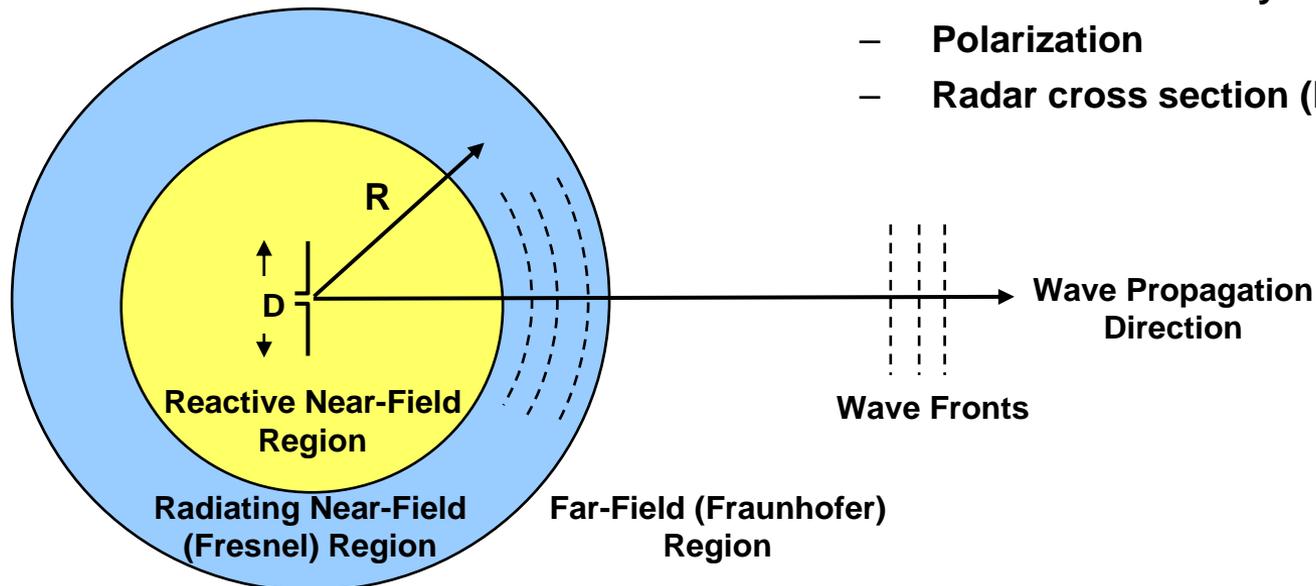
$$R < 0.62\sqrt{D^3/\lambda}$$

- Energy is stored in vicinity of antenna
- Near-field antenna quantities
  - Input impedance
  - Mutual coupling

## Far-field (Fraunhofer) Region

$$R > 2D^2/\lambda$$

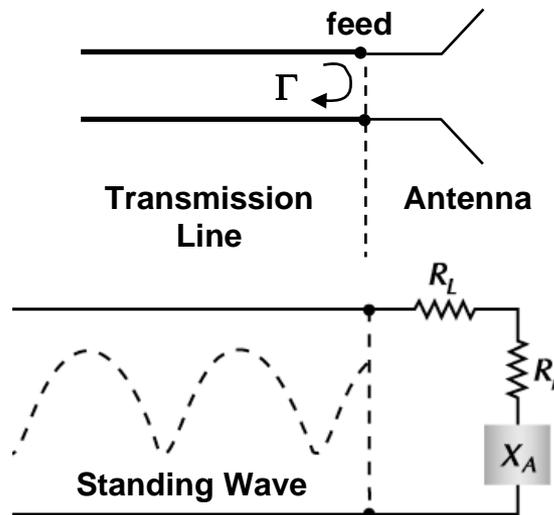
- All power is radiated out
- Radiated wave is a plane wave
- Far-field antenna quantities
  - Pattern
  - Gain and directivity
  - Polarization
  - Radar cross section (RCS)





# Antenna Input Impedance

- Antenna can be modeled as an impedance
  - Ratio of voltage to current at feed port
- Design antenna to maximize power transfer from transmission line
  - Reflection of incident power sets up standing wave
- Input impedance usually defines antenna bandwidth



$$\Gamma = 0$$

Incident Power  
is Delivered  
to Antenna

$$\Gamma = 1$$

All Incident  
Power is  
Reflected



# Outline

- Introduction
- Fundamental antenna concepts
- ➔ • Reflector antennas
- Phased array antennas
- Summary



# Parabolic Reflector Antenna

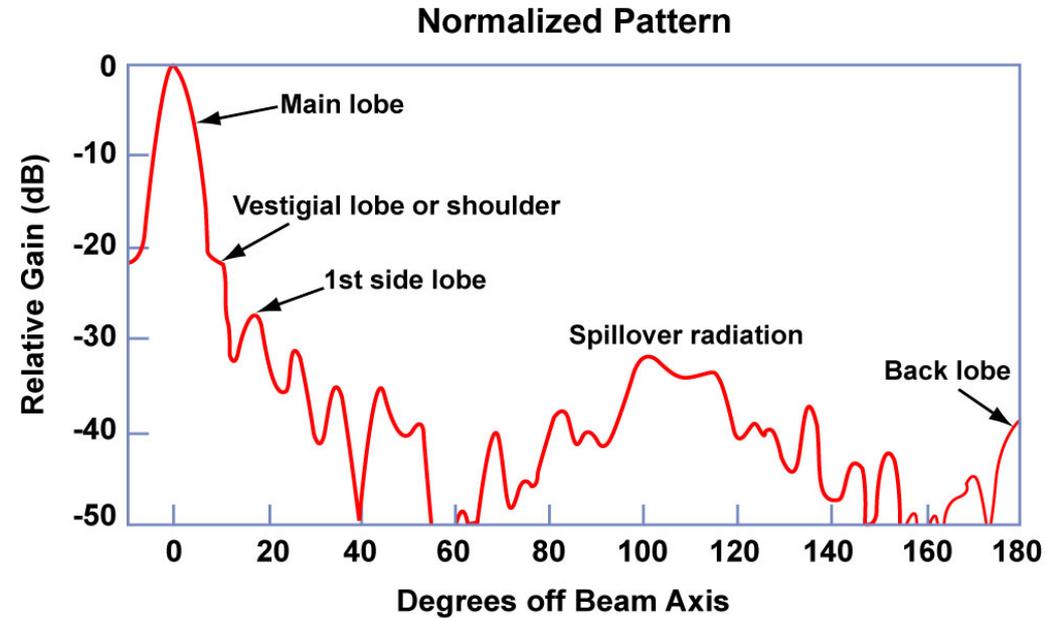
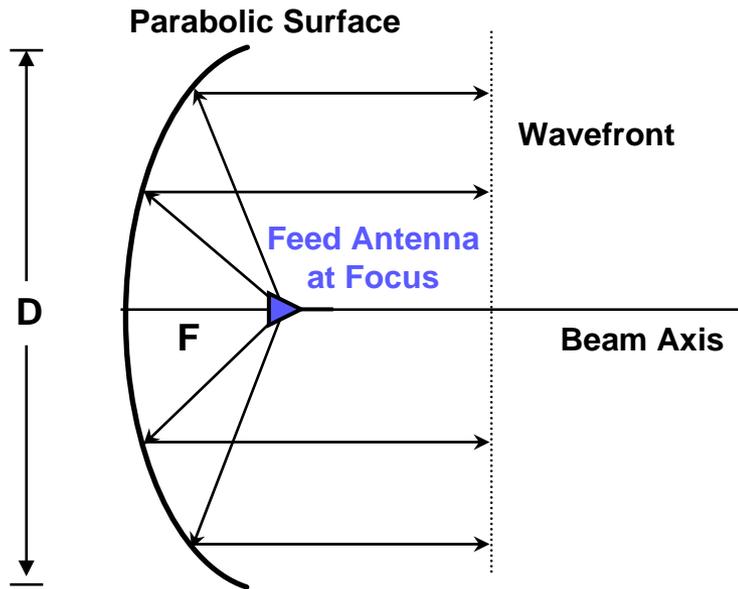
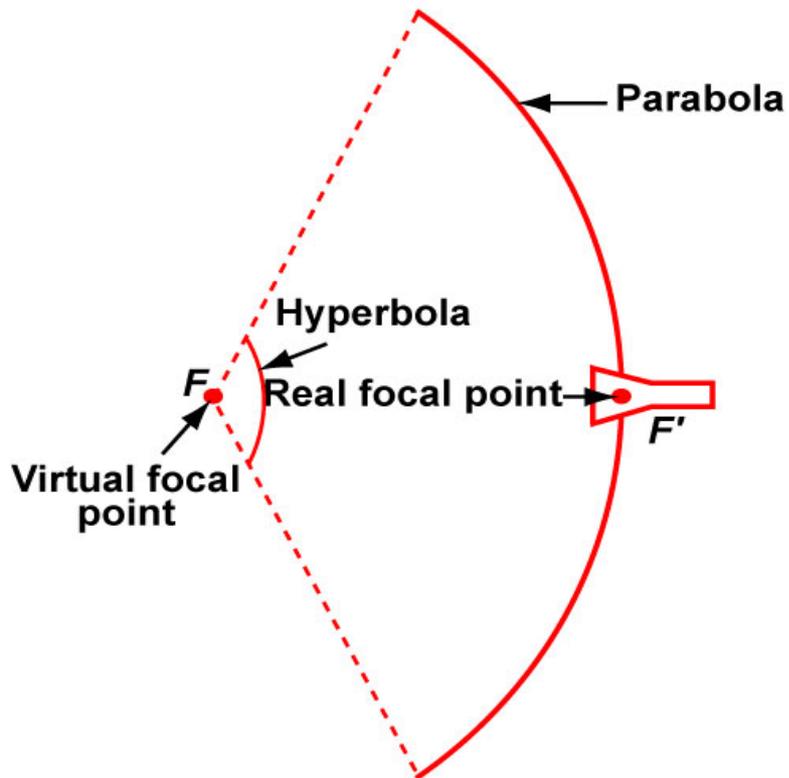


Figure by MIT OCW.

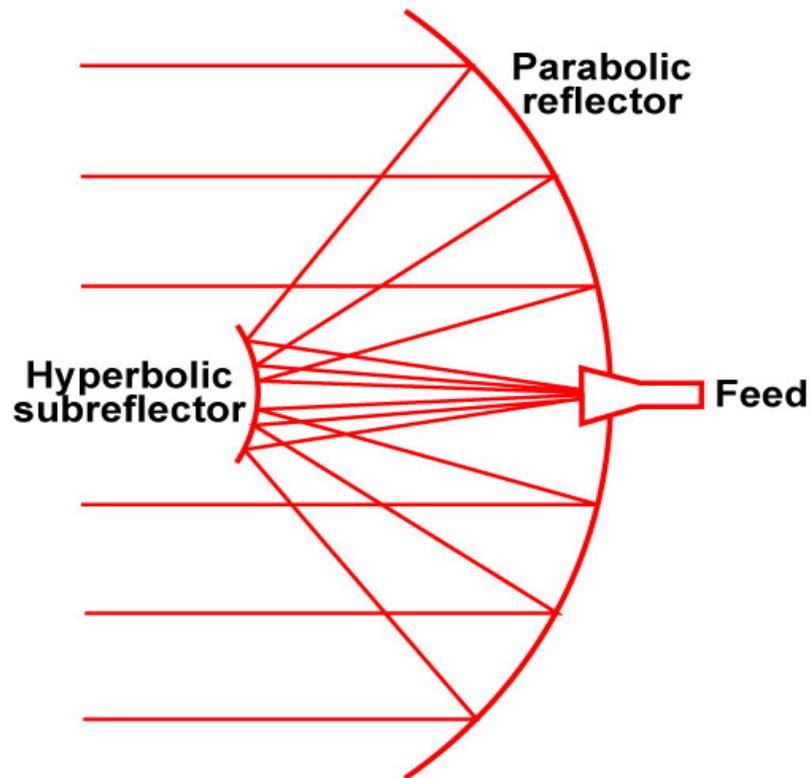
- Design is a tradeoff between maximizing dish illumination and limiting spillover
- Feed antenna choice is critical



# Cassegrain Reflector Antenna



**Geometry of Cassegrain Antenna**



**Ray Trace of Cassegrain Antenna**

Figure by MIT OCW.



# ALTAIR



**Dual frequency**

**VHF Parabolic**

**UHF Cassegrain**

**FSS (Frequency Selective Surface) used for reflector**



# Outline

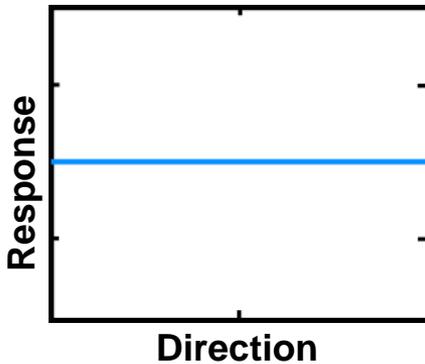
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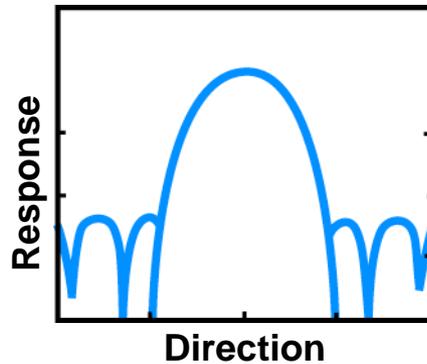
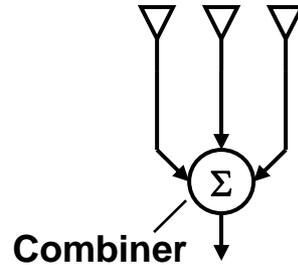
# Arrays

- Multiple antennas combined to enhance radiation and shape pattern

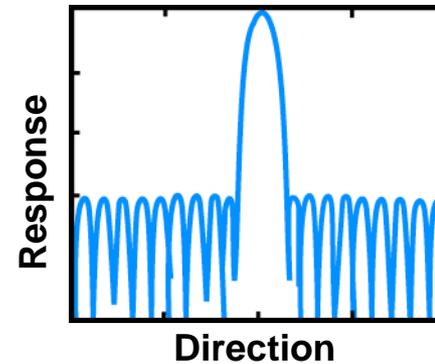
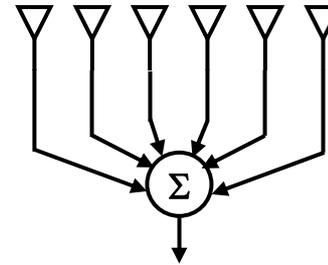
Isotropic Element



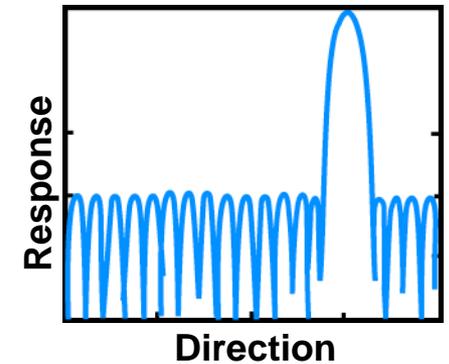
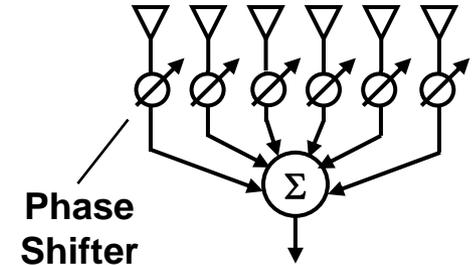
Array



Array



Phased Array



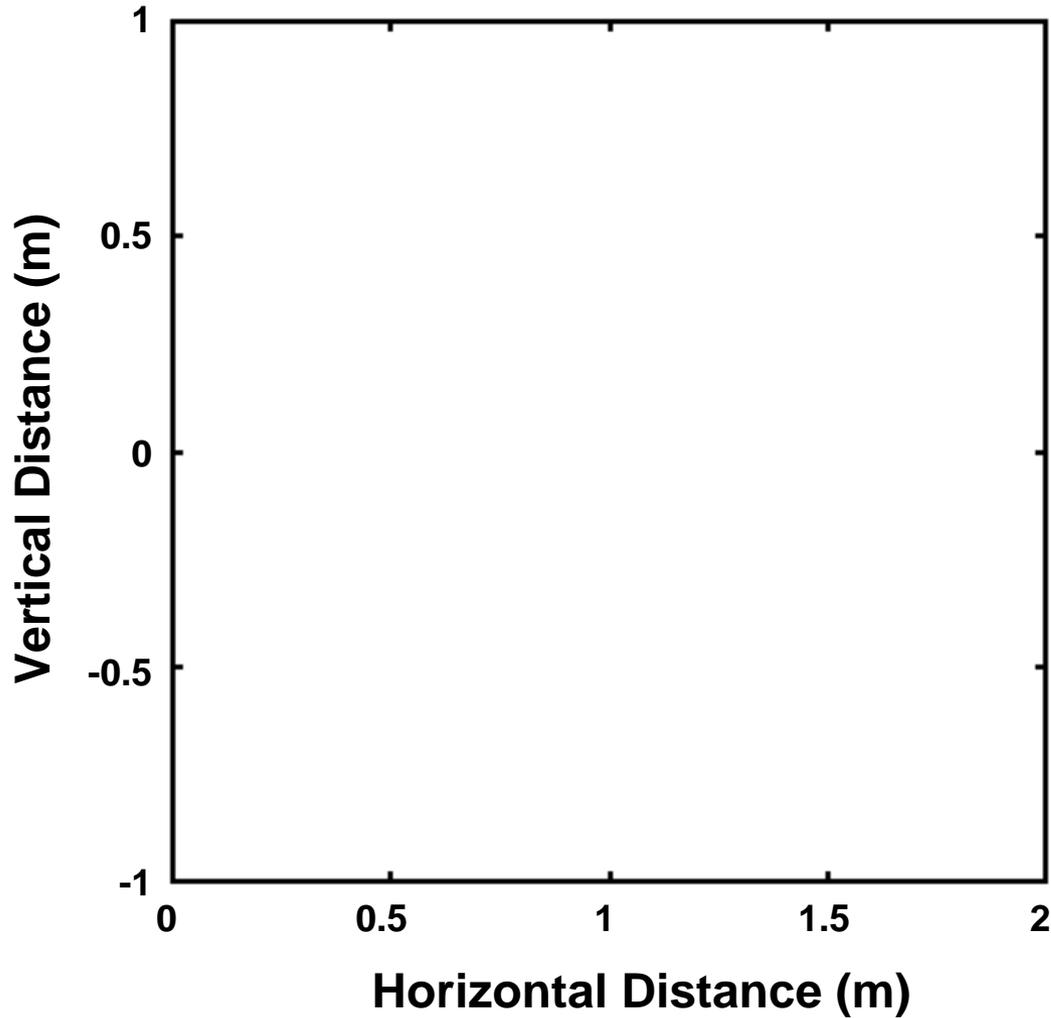


# Two Antennas Radiating

Dipole 1\* →

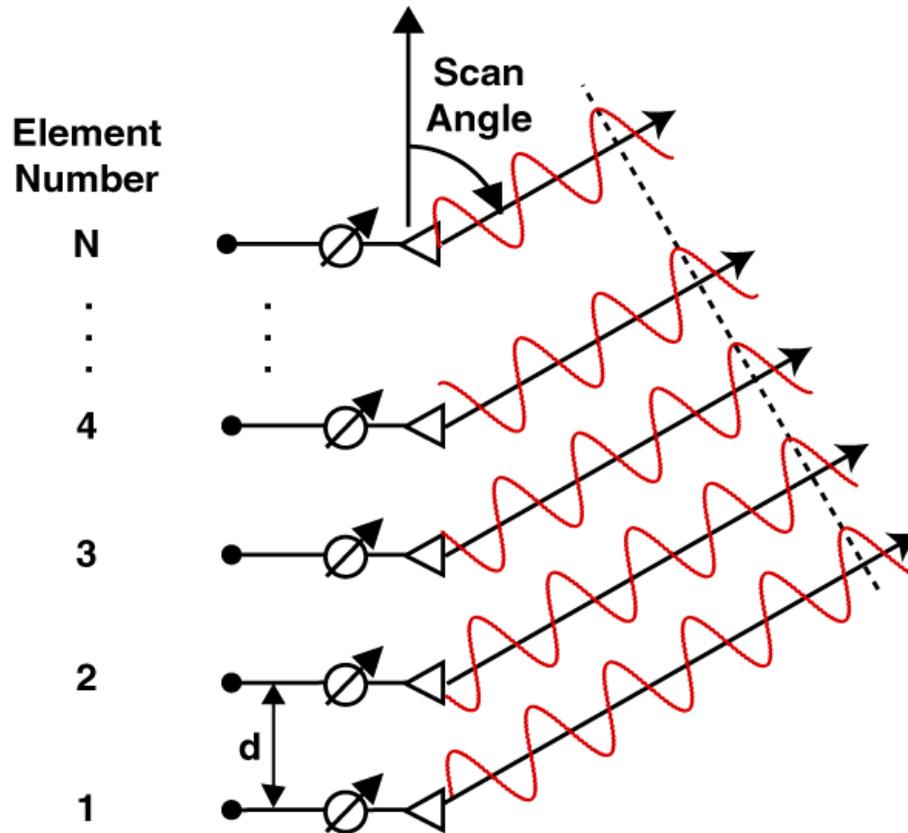
Dipole 2\* →

\*driven by  
oscillating  
sources  
(in phase)





# Array Controls



- **Geometrical configuration**
  - Linear, rectangular, triangular, circular grids
- **Element separation**
- **Phase shifts**
- **Excitation amplitudes**
  - For sidelobe control
- **Pattern of individual elements**
  - Isotropic, dipoles, etc.



# Increasing Array Size by Adding Elements

Linear Broadside Array  
Isotropic Elements  
 $\lambda/2$  Separation  
No Phase Shifting

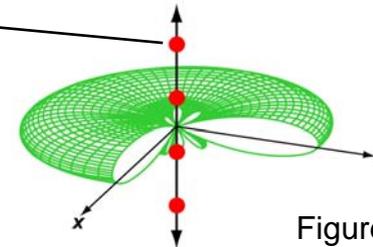
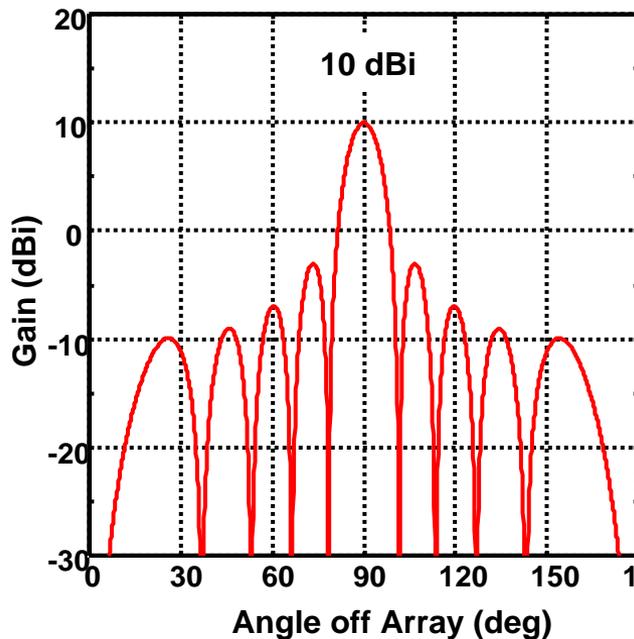
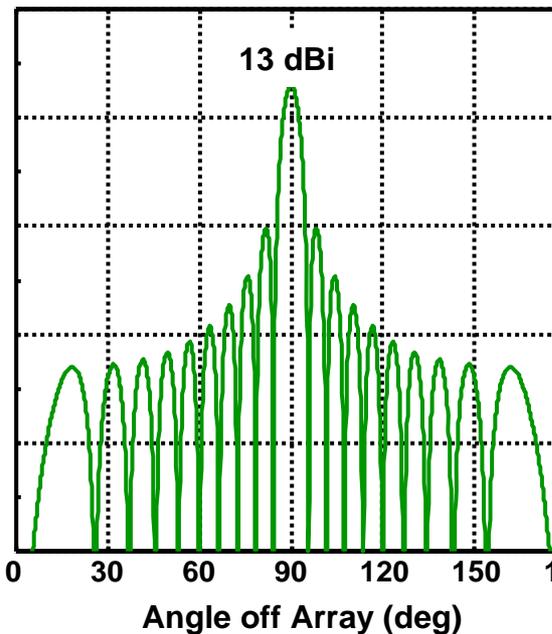


Figure by MIT OCW.

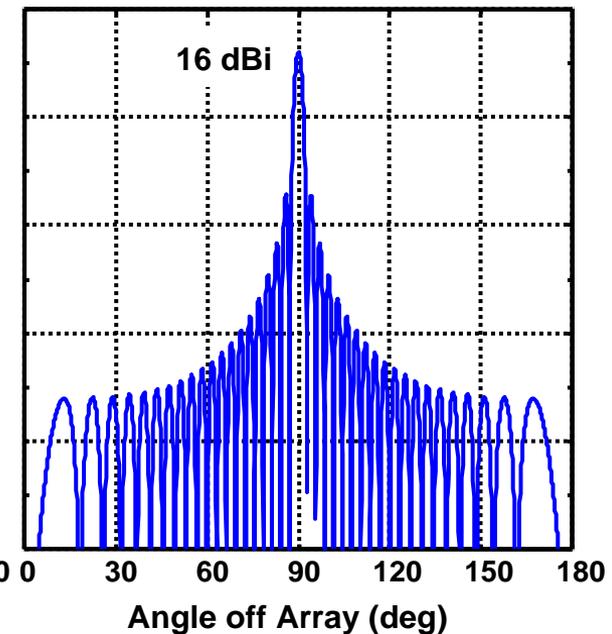
N = 10 Elements



N = 20 Elements



N = 40 Elements

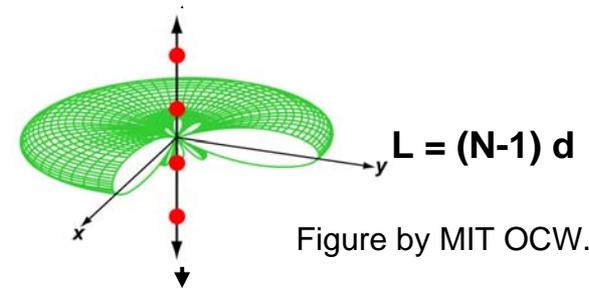


- Gain  $\sim 2N(d / \lambda)$  for long broadside array

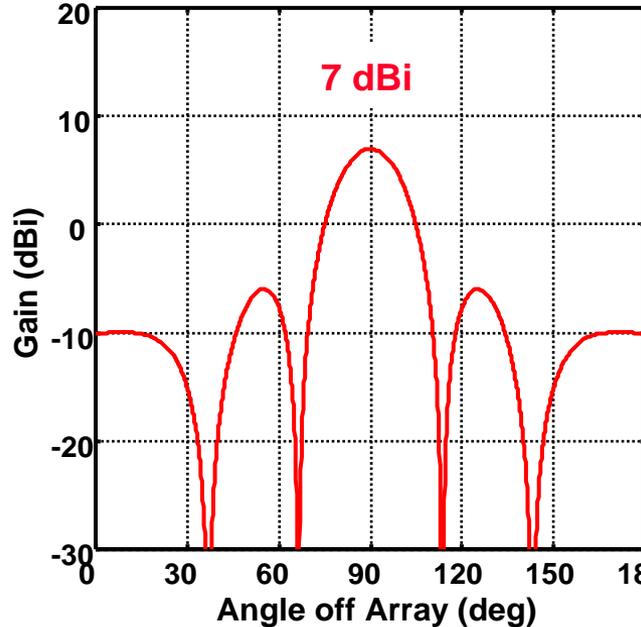


# Increasing Array Size by Separating Elements

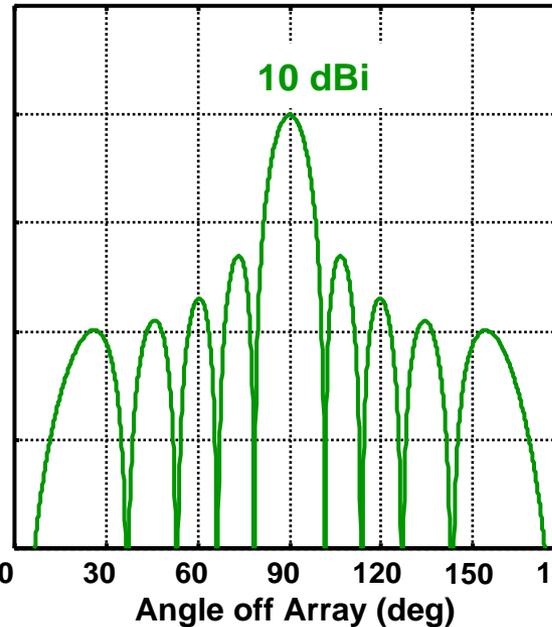
- Linear Broadside Array
- $N = 10$  Isotropic Elements
- No Phase Shifting



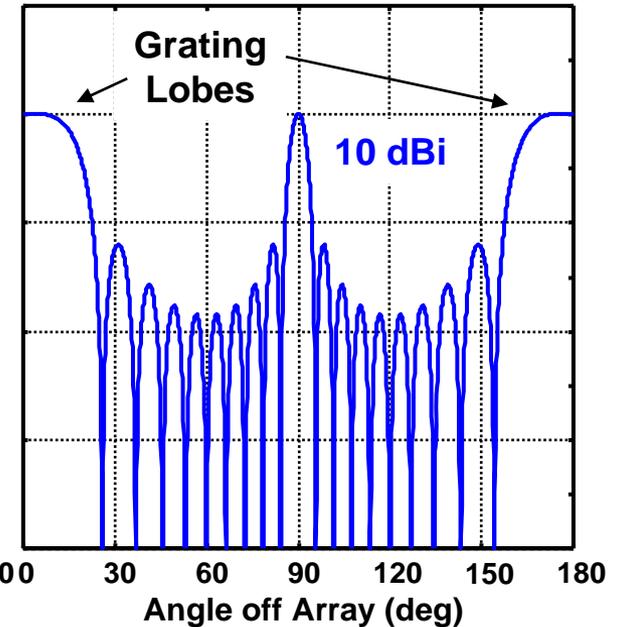
$d = \lambda/4$  separation



$d = \lambda/2$  separation



$d = \lambda$  separation

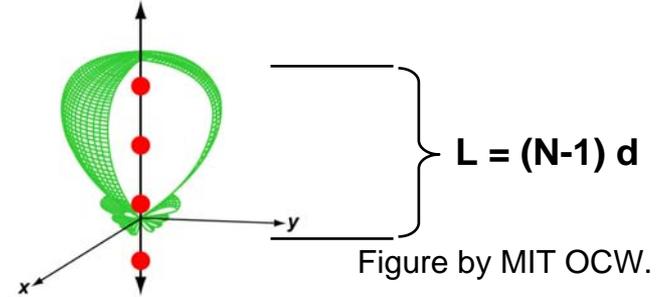


**Limit element separation to  $d < \lambda$  to prevent grating lobes for broadside array**

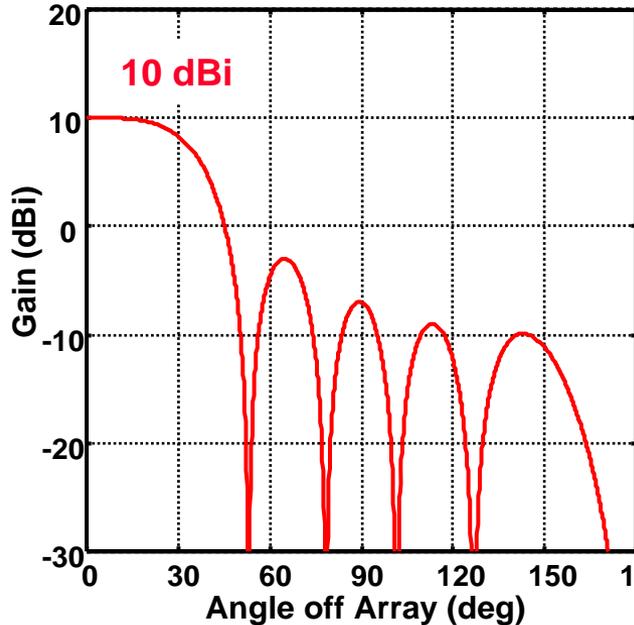


# Increasing Array Size of Scanned Array by Separating Elements

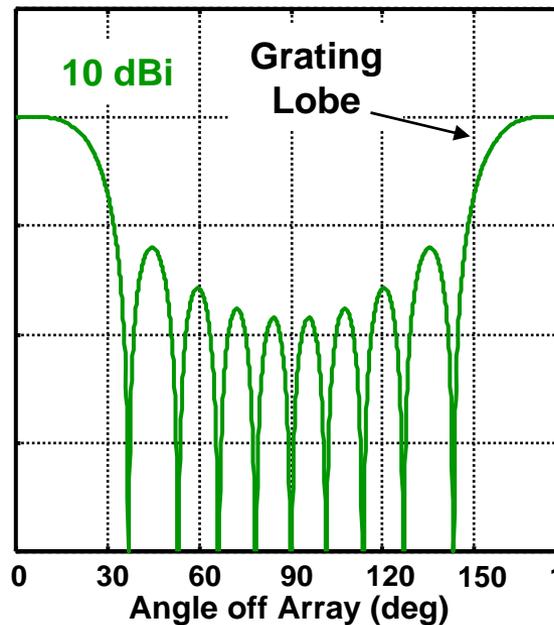
- Linear Endfire Array
- $N = 10$  Isotropic Elements
- Phase Shifted to Point Up



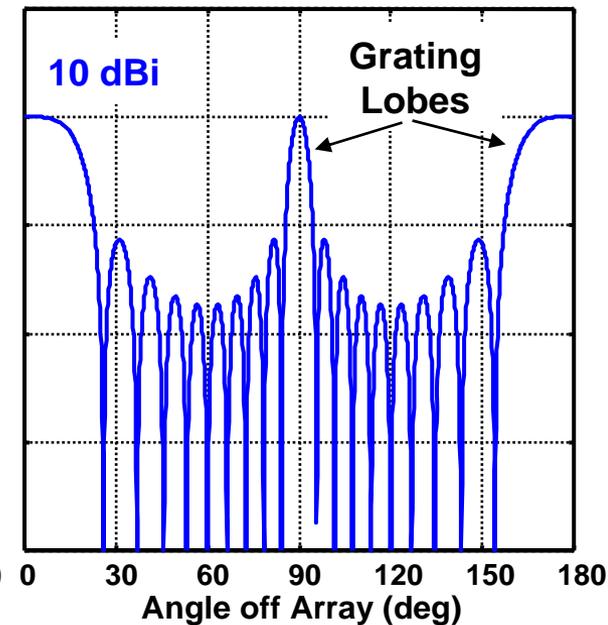
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$d = \lambda/2$  separation



$d = \lambda$  separation

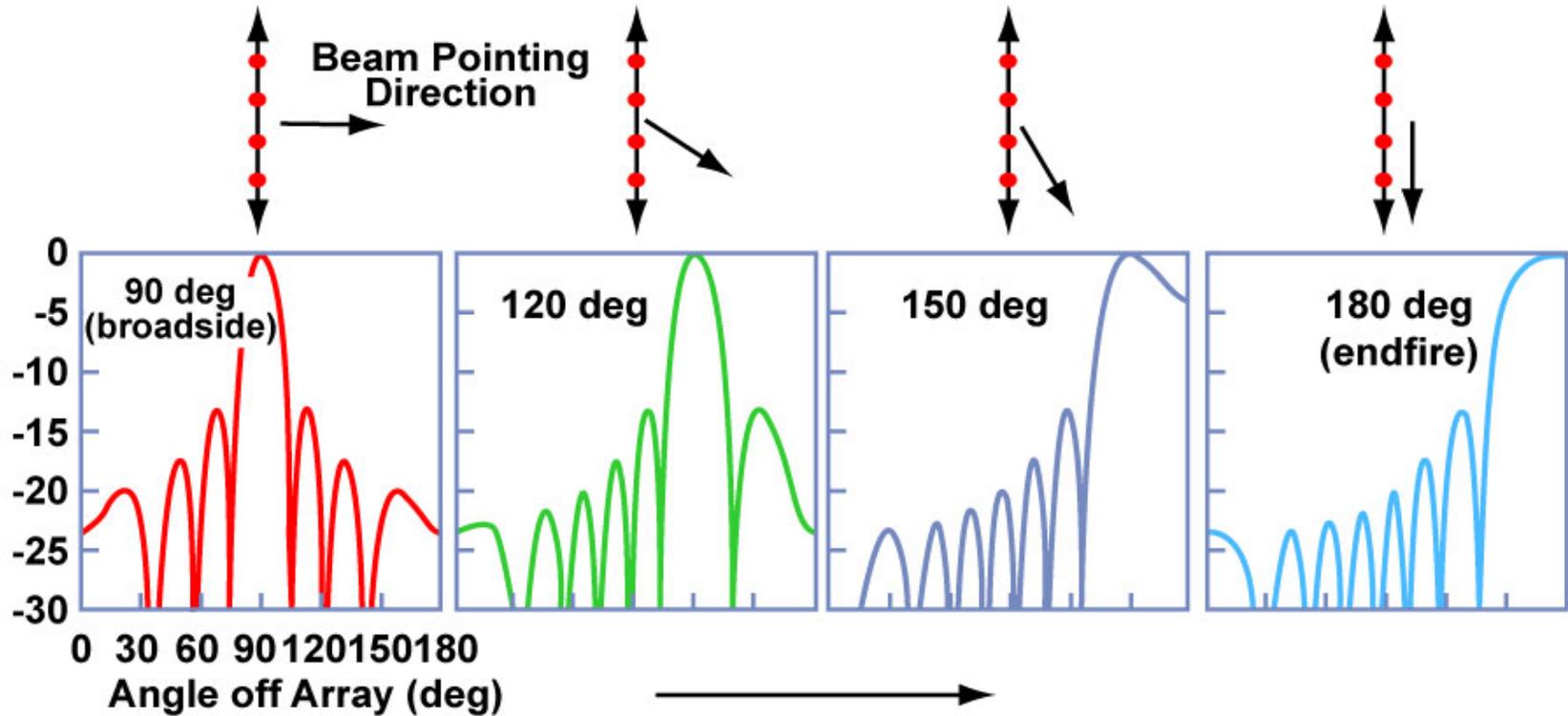


- No grating lobes for element separation  $d < \lambda / 2$
- Gain  $\sim 4N(d / \lambda) \sim 4L / \lambda$  for long endfire array *without grating lobes*



# Linear Phased Array

Scanned every 30 deg,  $N = 15$ ,  $d = \lambda/4$



Beamwidth increases as scan off broadside

Figure by MIT OCW.

To scan over all space without grating lobes,  
keep element separation  $d < \lambda / 2$



# Planar Arrays

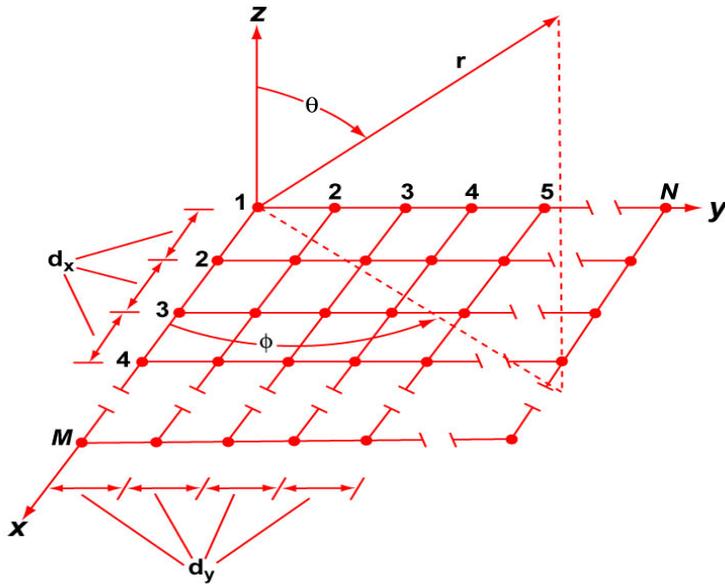


Figure by MIT OCW.

## Pattern No Scanning

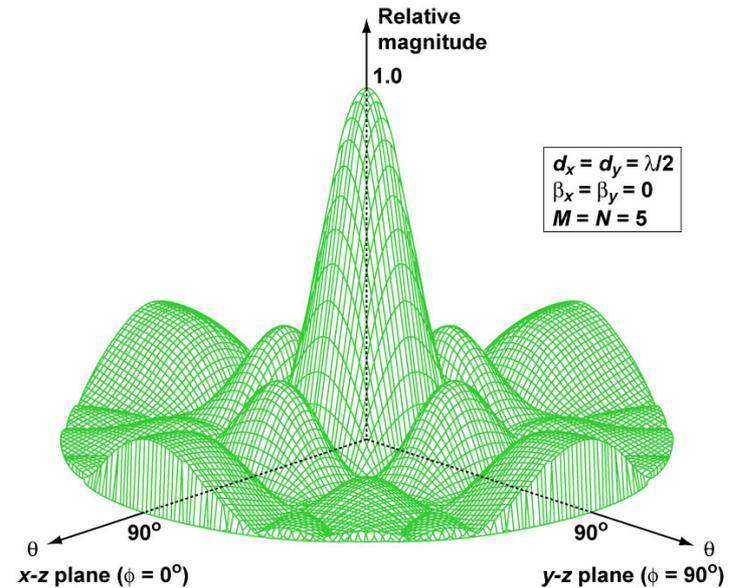


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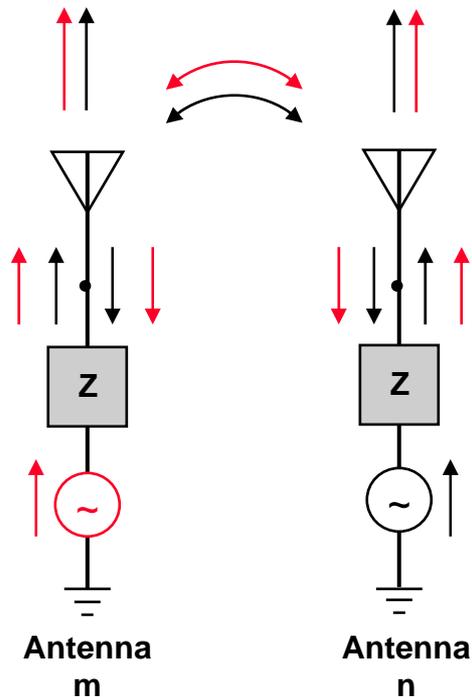
- **As scan to  $\theta_o$  off broadside:**
  - Beamwidth broadens by  $1/\cos\theta_o$
  - Directivity decreases by  $\cos\theta_o$

**To scan over all space without grating lobes,  
keep element separation in both directions  $< \lambda / 2$**



# Mutual Coupling

## Drive Both Antennas



- **Effect of one element on another**
  - Near-field quantity
  - Makes input impedance dependent on scan angle
- **Can greatly complicate array design**
  - Hard to deliver power to antennas for all scan angles
  - Can cause *scan blindness* where no power is radiated
- **Can limit scan volume and array bandwidth**

**But... mutual coupling can sometimes be exploited to achieve certain performance requirements**



# Phased Arrays vs Reflectors

- **Phased arrays provide beam agility and flexibility**
  - **Effective radar resource management (multi-function capability)**
  - **Near simultaneous tracks over wide field of view**
- **Phased arrays are significantly more expensive than reflectors for same power-aperture**
  - **Need for 360 deg coverage may require 3 or 4 filled array faces**
  - **Larger component costs**
  - **Longer design time**



# Outline

- Introduction
- Fundamental antenna parameters
- Reflectors
- Phased arrays
- ➔ • Summary



# Summary

- **Fundamental antenna parameters and array topics have been discussed**
  - Radiation
  - Gain, pattern, sidelobes, beamwidth
  - Polarization
  - Far field
  - Input impedance
  - Array beamforming
  - Array mutual coupling
- **Reflector antennas offer a relatively inexpensive method of achieving high gain for a radar**
  - Parabolic reflectors
  - Cassegrain feeds
- **Phased array antennas offer beam agility and flexibility in use**
  - But much more expensive than reflector antennas



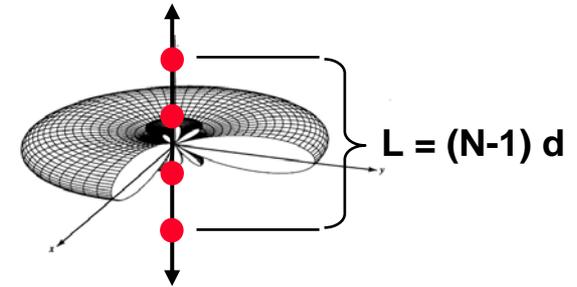
# References

- **Balanis, C. A., Antenna Theory: Analysis and design, 2<sup>nd</sup> Edition, New York, Wiley, 1997**
- **Skolnik, M., Introduction to Radar Systems, New York, McGraw-Hill, 3<sup>rd</sup> Edition, 2001**
- **Mailloux, R. J., Phased Array Antenna Handbook, Norwood, Mass., Artech House, 1994**

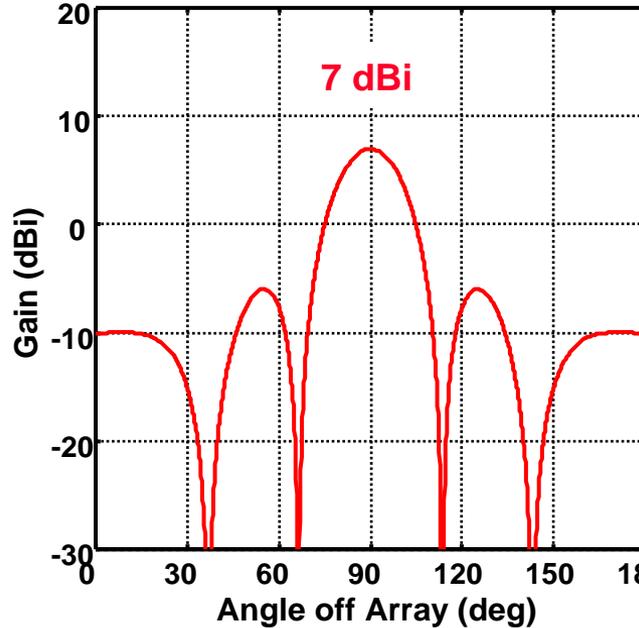


# Increasing Array Size by Separating Elements

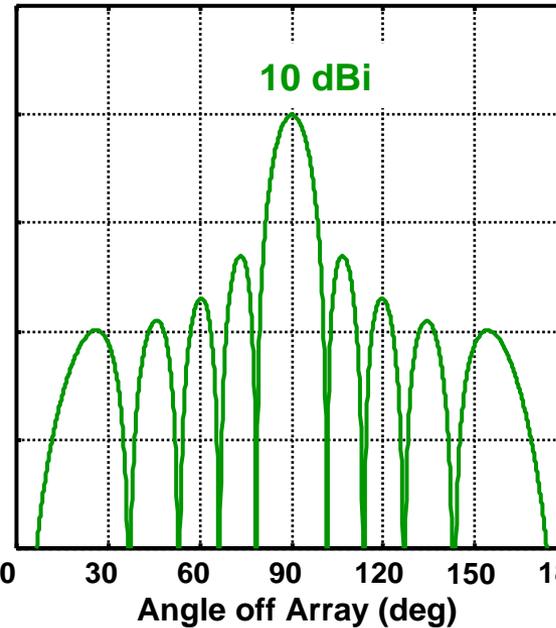
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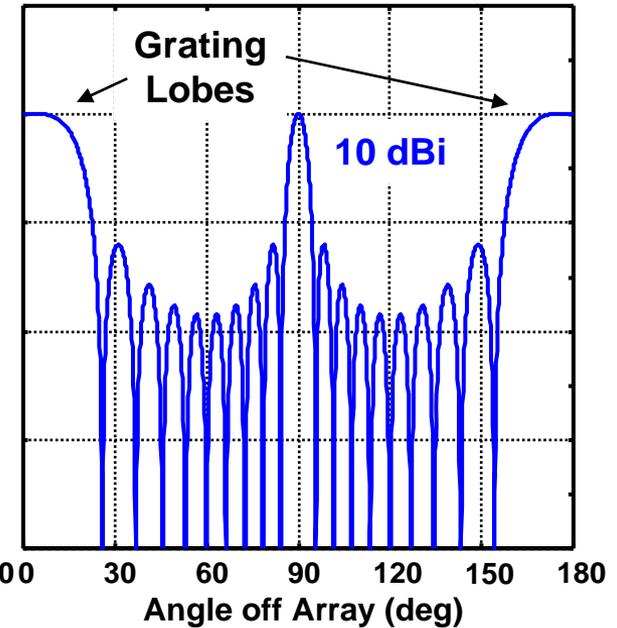
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$d = \lambda/2$  separation



$d = \lambda$  separation

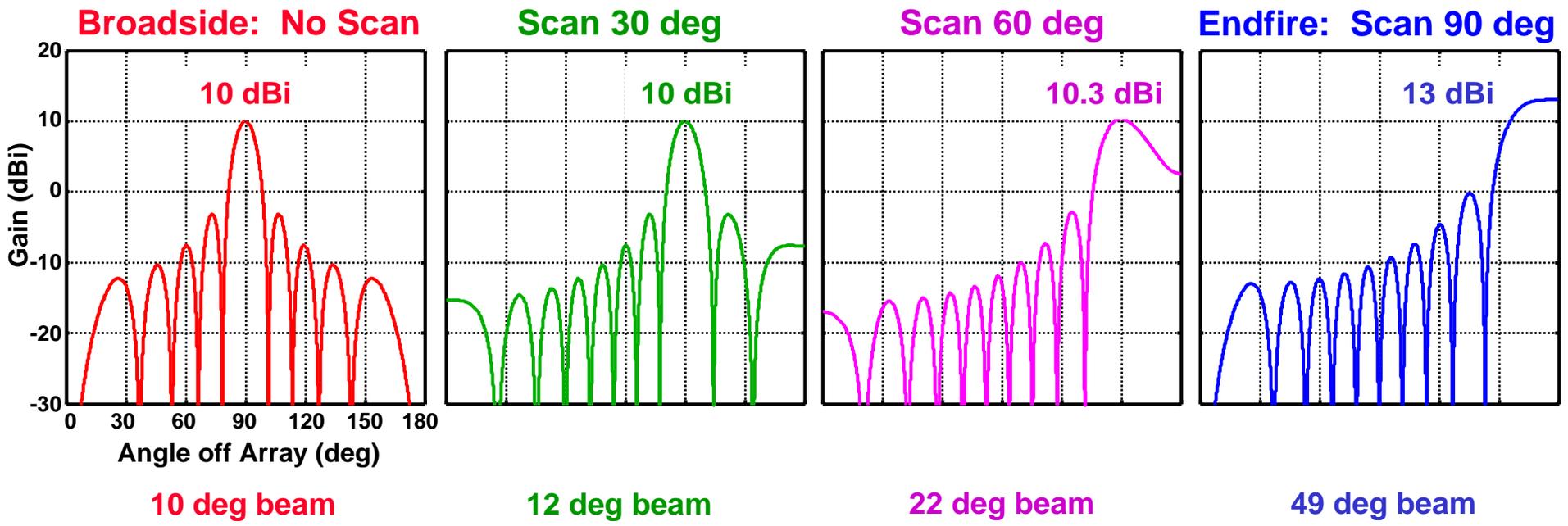


Limit element separation to  $d < \lambda$  to prevent grating lobes for broadside array



# Linear Phased Array

## Scanned every 30 deg, $N = 20$ , $d = \lambda/4$



**To scan over all space without grating lobes,  
keep element separation  $d < \lambda / 2$**